

HOMEWORK SET #4

Note: Please show all the steps leading to the final answer.

1. Show that by letting $l = \lambda/2$, equation (1) on page 26 of chap4 slide reduces to equation (2) on page 32.
2. Derive equation (3) on page 38 of chap4 slide.
3. A horizontal infinitesimal electric dipole of constant current I_0 is placed symmetrically about the origin and directed along the x axis. Derive
 - (a) far-zone fields (\mathbf{E} and \mathbf{H}) radiated by the dipole
 - (b) maximum directivity of the antenna
4. Repeat the previous problem for an infinitesimal magnetic dipole of constant magnetic current M_0 .
5. A half-wavelength dipole is radiating into free-space. The coordinate system is defined so that the origin is at the center of the dipole and the z -axis is aligned with the dipole. Input power to the dipole is 100 W. Assuming an overall efficiency of 50%, find the power density (in W/m^2) at $r = 500$ m, $\theta = 60^\circ$ and $\phi = 0^\circ$.